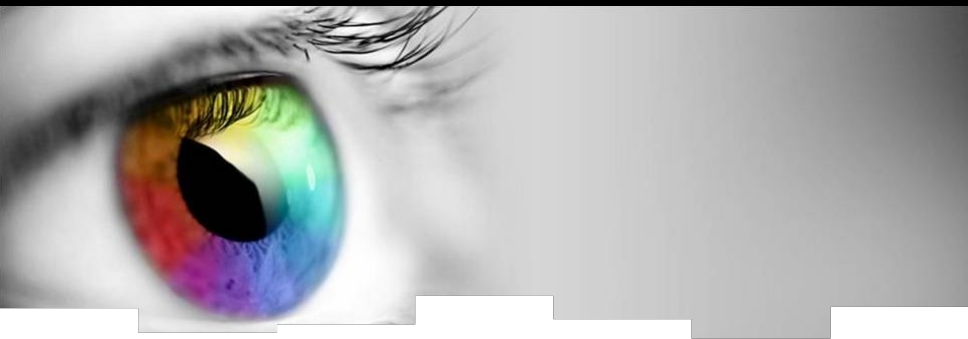


Tancredi Lepoint (S.C.C.I. 2011)



10-th birthday S.C.C.I, September 12, 2011



Presentation

■ Scholarship

- Master 1 Pure Mathematics (2009 – 2010)
- Master 2 **S.C.C.I** (2010 – 2011)

■ Internship at **Technicolor**

Internship Subject

How to design a white-box implementation for an asymmetric cryptographic primitive?

Presentation

■ Scholarship

- Master 1 Pure Mathematics (2009 – 2010)
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How to design a **white-box** implementation for an **asymmetric** cryptographic primitive?

White-Box Cryptology Motivations

- **Malicious software** on the user machine: search entropy

(Shamir and Van Someren, 1999)



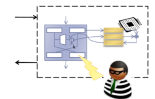
Keys need to be chosen at random (high entropy); code contains structure (low entropy)

- **DRM**: main application is to secure distribution of 'valuable' content. Decryption routine:
 - Hardware (e.g., set-top box)
 - Software (e.g., iTunes)

Platforms cannot be trusted

White-Box Model

- Powerful adversary: possible to **view** and **alter at will** the algorithm and the dynamic execution environment
- Goal: protect the key on an unsecure environment
- **Worse possible model**



Security

A implementation secured against WB attacks **is secure** against BB attacks and existant and *any future* GB attacks

Symmetric primitives (1)

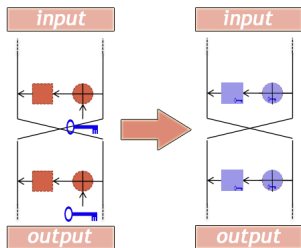
- State-of-the-art: symmetric primitives (AES and DES, Chow *et al.* in 2002)
- Technique for **hiding** secret keys in **software** implementation

Operation

Rewrite a **key-instantiated** version of a block cipher

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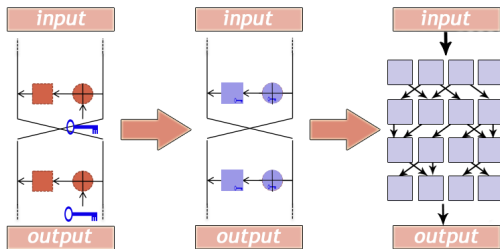


Operation

Rewrite a **key-instantiated** version of a block cipher

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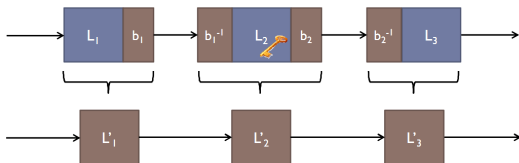
Operation

Transform into a **randomized** network of key-instantiated look-up tables

Symmetric primitives (2)

Operation

Randomization and delinearization



Patent of Irdeto

- White-Box implementation of RSA?

Main idea

Add a multiple of $\phi(N)$ to private key d :

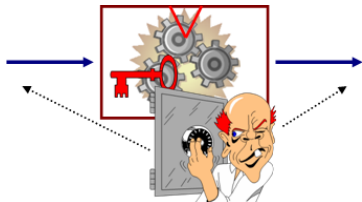
$$d^* = d + k\phi(N), \quad k > 0$$

Remarks

- **Contribution:** Broken with Miller's algorithm in WB context
- Not a new idea: used in smart-card

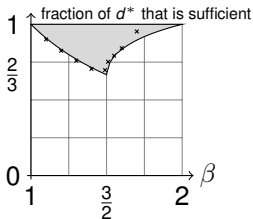
In grey-box context?

- Partial Key Exposure attacks when $d > N$

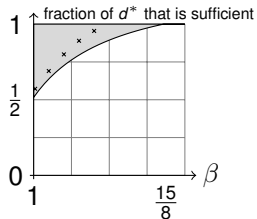


Contributions

Attacks when MSBs or LSBs are known



MSB



LSB



Ideas for asymmetric primitives

- Tabularizing the exponentiation (RSA, El-Gamal, . . .)
 - Use of the RNS
 - combined with Montgomery Modular Multiplication
- Tabularizing the polynomial modular multiplication
 - Spectral arithmetic

Problem

At one point: LUTs not possible, and cannot be obfuscated easily

- But **reduction** of WB implementation of RSA to **WB implementation of basis extension**

Conclusion

Contributions

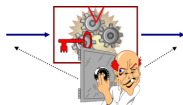
- White-box implementation (of RSA) **reduced** to implement basis extension in a WB fashion
- **Attack** on a patent of Irdeto (with Miller's algorithm)
- **Theorems** on MSBs and LSBs attacks
- **Design** of a software decoder to allow traitor tracing

Keywords

White-box, grey-box, lattices, traitor tracing, RNS, Montgomery multiplication, spectral arithmetic

Produced Papers

- *Traitor Tracing Schemes for Protected Software Implementations* (with Marc Joye), **to appear** in *11th ACM Workshop on Digital Rights Management (ACM-DRM 2011)*, Chicago, USA, October 21, 2011;
- Patent application #11305865.5, *TRAITOR TRACING FOR SOFTWARE-IMPLEMENTED DECRYPTION ALGORITHMS* (with Marc Joye), **filed** on July 6, 2011;
- *Partial Key Exposure on RSA with Private Exponents Larger than N* (with Marc Joye), **submitted for publication.**



Comments/Questions?



Thank you!